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## Connecticut State Teachers' Retirement System Experience Study for the

Five-Year Period Ending June 30, 2010


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Cavanaugh Macdonald
C ONSULTING, LLC
The experience and dedication you deserve

April 7, 2011
Teachers' Retirement Board
State of Connecticut
765 Asylum Avenue
Hartford, CT 06105
Dear Members of the Board:

We are pleased to submit the results of a study of the economic and demographic experience for the Connecticut Teachers' Retirement System. The purpose of this study is to assess the reasonability of the actuarial assumptions and methods for the System. The actuarial assumptions are used by the actuary to provide a best estimate of the value of all benefits expected to be paid by the System over future years. The valuation uses various methods in determining the required funding necessary to accumulate a sufficient amount of assets to fully fund the expected benefit payments.

This experience study covers the five-year period from July 1, 2005 to June 30, 2010. As a result of the study, it is recommended that revised assumptions be adopted by the Board for future use. Changing assumptions will not change the actual cost of future benefits but will impact the measurement of the expected value of future benefits and the required contributions to maintain actuarial soundness.

The experience study includes all active and inactive members including retired members, disabled members and beneficiaries of deceased members. The demographic experience was studied separately for males and females where gender is a basis for material differences in experience.

This report shows comparisons between the actual and expected cases of separation from active service, actual and expected number of deaths, and actual and expected salary increases. Tables and graphs are used to show the actual rates measured, the rates expected under the current assumptions and, where applicable, the proposed change to rates.

The recommended decrement tables are shown in Appendix A of this report. In the actuary's judgment, the recommended rates are suitable for use until further experience indicates that modifications are needed.

## Teachers' Retirement Board

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The experience study was performed by, and under the supervision of, independent actuaries who are members of the American Academy of Actuaries with experience in performing valuations for public retirement systems and who meet the Qualification Standards of the American Academy of Actuaries to render the actuarial opinion contained herein.

Respectfully submitted,


John J. Garrett, ASA, FCA, MAAA Principal and Consulting Actuary


Cathy Turcot Principal and Managing Director


Jonathan T. Craven, ASA, EA, FCA, MAAA
Senior Actuary

## Board Summary

The following table summarizes the findings and recommendations with regard to the actuarial assumptions and methods utilized for actuarial valuations of the Connecticut Teachers' Retirement System. Detailed explanations for the recommendations are found in the sections that follow.

|  | Summary of Recommended Assumptions |
| :---: | :---: |
| Economic Assumptions |  |
| Rates of Salary Increase | Composed of Inflation component, Real Rate of Wage Increase component and a Service Based Scale. |
| Inflation | Recommend no change to the 3.00\% rate of inflation. |
| Real Rate of Wage Increase | Recommend a decrease in the annual rate of real wage increase assumption from $1.00 \%$ to $0.75 \%$. |
| Service Based | Recommend minor changes to the current service based rates. Also recommend use of a modified assumption for expected salary increases for 2010 though 2012. |
| Investment Rate of Return | Composed of Inflation component ( $3.00 \%$ from above) and Real Rate of Return component which is currently $5.50 \%$. We find the $8.50 \%$ to be within the reasonable range for a long-term investment return assumption and have provided results using an $8.25 \%$ assumption for consideration. |
| Payroll Growth | Recommend change from $4.00 \%$ to $3.75 \%$ based upon the sum of the inflation and real rate of wage increase. |
| Demographic Assumptions |  |
| Withdrawal | Recommend minor change only to male rates at ages 55 to 59. |
| Retirement | Recommend change to current assumption for early retirement only. |
| Mortality | Recommend no change to the current assumption. |
| Disability | Recommend no change to the current assumption. |
| Marriage Assumption | Recommend no change to the current assumption. |
| Actuarial Methods |  |
| Actuarial Cost Method | Recommend no change to the current method. |
| Asset Smoothing | Recommend no change to the current method. |
| Amortization Method | Recommend no change to the current method. |

## Impact on Valuation Results

The following table highlights the impact of the recommended changes on the June 30, 2010 actuarial valuation results.

| Impact on Principal Valuation Results <br> (Dollar amounts in thousands) |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | Valuation Results 2010 | Results with Recommended Assumptions using $8.50 \%$ Investment Return | Change in Results | Results with Recommended Assumptions using 8.25\% Investment Return | Change in Results |
| Normal Cost Rate | 10.11\% | 9.83\% | (0.28\%) | 10.44\% | 0.33\% |
| Funded Ratio | 61.4\% | 61.6\% | 0.2\% | 60.1\% | (1.3\%) |
| Unfunded Actuarial Accrued Liability | \$9,065,729 | \$8,976,831 | $(\$ 88,898)$ | \$9,574,107 | \$508,378 |
| Employer Annual Required Contribution Rate | 19.20\% | 19.24\% | 0.04\% | 20.46\% | 1.26\% |
| Expected FYE 2012 Employer Required Contribution | \$757,246 | \$755,224 | (\$2,022) | \$802,990 | \$45,744 |

There are three economic assumptions used in the actuarial valuations performed for the System. They are:

- Investment Rate of Return
- Rates of Wage Inflation
- Rate of Payroll Growth

Each of these assumptions is separated into its relevant component parts. The investment rate of return assumption is comprised of an inflation component and a real rate of return component. Similarly the rate of wage inflation assumption is comprised of an inflation component, a real rate of wage increase component (also called the productivity component). Finally, the payroll growth assumption uses the components for inflation and real wage increases in determining a reasonable range for annual growth in total payroll. The actuary is tasked with defining a reasonable range and, where appropriate, recommending a best estimate for each of the economic assumptions.

The Actuarial Standards Board has issued Actuarial Standard of Practice (ASOP) No. 27, "Selection of Economic Assumptions for Measuring Pension Obligations", which provides guidance to actuaries in selecting economic assumptions for measuring obligations under defined benefit plans. As noted in ASOP No. 27, because no one knows what the future holds, the best an actuary can do is to use professional judgment to estimate possible future economic outcomes based on a mixture of past experience and future expectations. These estimates therefore are best stated as a range utilizing the actuary's professional judgment. In setting the range and the single point within that range to use, the actuary should consider a number of factors, including the purpose and nature of the measurement, and appropriate recent and long-term historical economic data. However, the standard explicitly advises the actuary not to give undue weight to recent experience.

Each economic assumption should individually satisfy this standard. Furthermore, with respect to any particular valuation, each economic assumption should be consistent with every other economic assumption over the measurement period.

In our opinion, the economic assumptions recommended in this report have been developed in accordance with ASOP No. 27.

## Section II: Economic Assumptions

## Inflation

The assumed rate of inflation is the expectation of the long-term annual rate of increase in the Consumer Price Index and is a component of all economic assumptions. This is also called price inflation.

It is important that the inflation assumption be consistently applied throughout the economic assumptions utilized in an actuarial valuation. This is called for in ASOP No. 27 and is also required to meet the parameters for determining pension liabilities and expense under Governmental Accounting Standards Board (GASB) Statements No. 25 and 27.

The current set of assumptions as developed by the prior actuary does not explicitly set a price inflation assumption. However, in reading the prior experience study it appears that the $4.00 \%$ wage inflation assumption is comprised of $3.00 \%$ price inflation and $1.00 \%$ real wage increase assumptions.

Past Experience: The Consumer Price Index, US City Average, All Urban Consumers, CPI (U), has been used as the basis for reviewing historical levels of price inflation. The graph below shows the annual increases in the CPI ( U ) as of December 31st for each of the latest 50 years compared to the current assumed $3.00 \%$ rate of inflation.

Annual CPI (U) Increases 1961-2010


## Section II: Economic Assumptions

The table below provides historical annualized rates and annual standard deviation of the CPI-U over periods ending December $31^{\text {st }}$.

| Period | Annualized <br> Rate of Inflation | Annual Standard <br> Deviation |
| :---: | :---: | :---: |
| $1926-2010$ | $2.99 \%$ | $4.18 \%$ |
| $1950-2010$ | $3.65 \%$ | $2.96 \%$ |
| $1960-2010$ | $4.14 \%$ | $2.98 \%$ |
| $1970-2010$ | $4.39 \%$ | $3.18 \%$ |
| $1980-2010$ | $2.96 \%$ | $1.24 \%$ |
| $1990-2010$ | $2.47 \%$ | $0.92 \%$ |
| $2000-2010$ | $2.42 \%$ | $1.18 \%$ |

Over shorter historical periods, the average annual rate of increase in the CPI-U has been below $3.00 \%$. The period of high inflation from 1973 to 1982 has a significant impact on the averages over periods which include these rates. Further, the longest historic average rate of $2.99 \%$ is very close to the average rate of $2.96 \%$ over the prior 30 years (1980 to 2010) but the volatility of the annual rates in the more recent years has been markedly lower as indicated by the significantly lower annual standard deviations. Many experts attribute the lower average annual rates and lower volatility to the increased efforts of the Federal Reserve since the early 1980's to stabilize price inflation. We give greater weight to the 30 -year historical period in our analysis.

Additional information to consider is obtained from measuring the spread on treasury inflation protected securities (TIPS) and from the prevailing economic forecasts. The spread between the yield on treasury securities (bonds) and the inflation indexed yield on TIPS of the same maturity is referred to as the "breakeven rate of inflation" and represents the bond market's expectation of inflation over the period to maturity. The table below provides the calculation of the breakeven rate of inflation as of December 31, 2010.

| Years to <br> Maturity | Bond Yield | TIPS Yield | Breakeven Rate of <br> Inflation |
| :---: | :---: | :---: | :---: |
| 10 | $3.30 \%$ | $1.00 \%$ | $2.30 \%$ |
| 20 | $4.13 \%$ | $1.59 \%$ | $2.54 \%$ |
| 30 | $4.34 \%$ | $1.86 \%$ | $2.48 \%$ |

The bond market's expectation for the rate of inflation over the longer term is approximately $2.50 \%$ which is significantly lower than long term historical average annual rates. Additionally, based upon information contained in the "Survey of Professional Forecasters" for the fourth quarter of 2010 as published by the Philadelphia Federal Reserve Bank, the mean expected
annual rate of inflation for the ten years beginning January 1, 2011 is 2.20\%. Although 10 years of future expectation is too short of a period for the basis of our inflation assumption, the information does provide additional evidence that the consensus expectations of these experts are for significantly lower rates of inflation than the historical average for the near term future.

Recommendation: It is difficult to accurately predict inflation. Current economic forecasts and the bond market suggest lower inflation over the next ten to thirty years which is a shorter time period than appropriate for our purposes. In the 2010 OASDI Trustees Report, the Chief Actuary for Social Security bases the 75 year cost projections on an intermediate inflation assumption of $2.8 \%$ with a range of $1.8 \%$ to $3.8 \%$. We concur with a reasonable range of $2.0 \%-$ $4.0 \%$, and recommend continued use of a $3.00 \%$ per year rate of inflation.

| Price Inflation Assumption |  |
| :--- | :---: |
| Current | $3.00 \%$ |
| Reasonable Range | $2.00 \%-4.00 \%$ |
| Recommended | $3.00 \%$ |

## Investment Rate of Return

Background: The assumed investment return is one of the most significant assumptions in the annual actuarial valuation process as it is used to discount the expected future benefit payments for all active, inactive and retired members. Minor changes in this assumption can have a major impact on valuation results. The investment rate of return assumption should reflect the longterm average annual rate of return which can reasonably be expected based on the target asset allocation and capital market assumptions of the investment professionals.

The current assumption is $8.50 \%$, consisting of a price inflation assumption of $3.00 \%$ and a real rate of return (return net of inflation) assumption of $5.50 \%$.

Past Experience: The recent experience over the last 10 years is shown in the table below.

| Year Ending 6/30 | Market Value Rate of <br> Return |
| :---: | :---: |
| 2001 | $(3.71 \%)$ |
| 2002 | $(6.58 \%)$ |
| 2003 | $2.13 \%$ |
| 2004 | $15.34 \%$ |
| 2005 | $10.49 \%$ |
| 2006 | $11.08 \%$ |
| 2007 | $17.47 \%$ |
| 2008 | $(4.77 \%)$ |
| 2009 | $(17.84 \%)$ |
| 2010 | $13.45 \%$ |
| Average | $3.09 \%$ |

Historical returns over a short time period are not credible for the purpose of setting the longterm assumed future rate of return. Particular to this ten year period were two severe declines in the stock markets. In determining the reasonable range for this assumption we first look at longterm historical returns of broad market indices. We focus on the returns of stocks and highquality bonds because they are the two major components of the portfolio and have significant amounts of performance history.

Analysis: Utilizing the historical real rates of return of the S\&P 500 and the Intermediate Government Bond Index for the last 70 years, we determine the historical average annual rate of return of common allocation of large retirement funds ( $40 \%$ stocks $/ 60 \%$ bonds to $70 \%$ stocks $/ 30 \%$ bonds). On this basis the initial reasonable range for expected real rates of return is from $4.1 \%$ to $5.6 \%$. This correlates well with the latest information available in the Public Fund Survey which shows the most common plan real rate of return assumption of $5.0 \%$ with a median equity allocation of $52 \%$. We then add the recommended inflation assumption of $3.0 \%$ to the reasonable range of real returns. This results in an initial reasonable range for the long-term investment rate of return assumption of $7.1 \%$ to $8.6 \%$.

In recommending a reasonable range for the investment rate of return assumption, we also consider the capital market assumptions of investment professionals. We were provided by the State Treasurer's Office the most recent capital market assumptions and target asset allocation for our analysis. We use statistical methods to approximate the longer-term expectation of returns. The Actuarial Standards of Practice prescribe that a reasonable range for this assumption would be between the $25^{\text {th }}$ and $75^{\text {th }}$ percentile of long-term expected returns. Our
analysis produces a reasonable range for the long-term investment return assumption, net of expenses, between $6.4 \%$ and $9.1 \%$ as shown in the table below.

| Statistical Analysis of Expected Return Distribution |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\begin{gathered} \text { Time } \\ \text { Span } \\ \text { In } \\ \text { Years } \end{gathered}$ | Mean Rates of Return | Standard <br> Deviation | Rates of Return by Percentile |  |  |  |  |
|  |  |  | $5^{\text {th }}$ | $25^{\text {th }}$ | $50^{\text {dh }}$ | $75^{\text {th }}$ | $95^{\text {th }}$ |
| 1 | 8.7\% | 14.2\% | -13.0\% | -1.3\% | 7.8\% | 17.7\% | 33.5\% |
| 5 | 7.9\% | 6.3\% | -2.1\% | 3.6\% | 7.8\% | 12.1\% | 18.6\% |
| 10 | 7.9\% | 4.4\% | 0.7\% | 4.8\% | 7.8\% | 10.8\% | 15.3\% |
| 20 | 7.8\% | 3.1\% | 2.7\% | 5.7\% | 7.8\% | 9.9\% | 13.1\% |
| 30 | 7.8\% | 2.6\% | 3.6\% | 6.0\% | 7.8\% | 9.5\% | 12.1\% |
| 50 | 7.8\% | 2.0\% | 4.5\% | 6.4\% | 7.8\% | 9.1\% | 11.1\% |

We should note that the capital market assumptions produced by investment consultants vary over time. We recommend that we reassess the reasonable range with each significant future change to either the capital market assumptions or the asset allocations provided in the investment policy.

The most recent survey of large public plans, Public Fund Survey reported as of November 2010 by the National Association of State Retirement Administrators shows that most of the 126 funds surveyed have an $8.0 \%$ investment return assumption and 31 funds have a return assumption greater than $8.0 \%$ ( 13 funds use an $8.5 \%$ return assumption). Neither of the Connecticut statewide systems is included in the survey.

Recommendation: A blending of the reasonable range for the investment return assumption using the historical broad market basis $(7.1 \%$ to $8.6 \%)$ and the long-term reasonable range produced using the investment professional's capital market assumptions and target allocation of the System ( $6.4 \%$ to $9.1 \%$ ), results in the reasonable range to be from $6.8 \%$ to $8.9 \%$. We confirm that the current $8.50 \%$ assumption is within the reasonable range for this assumption, although at the higher-end of this range. For the Board's consideration we also provide the impact of reducing the investment rate of return assumption to $8.25 \%$.

| Investment Return Assumption |  |
| :--- | :---: |
| Current | $8.5 \%$ |
| Reasonable Range | $6.8 \%-8.9 \%$ |
| Recommended | $8.5 \%$ |
| Alternative for Consideration | $8.25 \%$ |

## Wage Inflation

Background: Wage inflation, thought of as the "across the board" rate of salary increases is comprised of the price inflation assumption combined with an assumption for the real rate of wage increases. The real rate of wage increase is the rate of increase in wages above price inflation. In constructing the rates of salary increases assumptions, the rate of wage inflation assumption is further combined with an assumption for service based salary increases. The service based salary increase assumption is provided in the demographic assumption section of the report. The current assumption implies the assumed real rate of wage increase is $1.00 \%$.

Past Experience: The Social Security Administration publishes data on wage growth in the United States. As with our analysis of inflation, we provide below wage inflation and a comparison with price inflation over various time periods. Since wage data is only available through 2009 we use that year as the end point.

| Period Ending 12/31/2009 | Average Annual <br> Rate of Wage <br> Inflation | Average Annual <br> Rate of Price <br> Inflation | Average Annual <br> Rate of Real Wage <br> Increase |
| :---: | :---: | :---: | :---: |
| 5 Years | $2.7 \%$ | $2.3 \%$ | $0.4 \%$ |
| 10 Years | $2.9 \%$ | $2.4 \%$ | $0.5 \%$ |
| 20 Years | $3.6 \%$ | $2.6 \%$ | $1.0 \%$ |
| 30 Years | $4.3 \%$ | $3.2 \%$ | $1.1 \%$ |
| 50 Years | $4.8 \%$ | $3.7 \%$ | $1.1 \%$ |

Over the past 5 years of experience data we analyzed, the apparent rate of real wage increases in the data was $0.82 \%$ which is based upon the average rate of salary increases above price inflation for active members with no apparent service based salary increases.

Recommendation: We develop the reasonable range to be $0.5 \%$ to $1.1 \%$, and recommend use of a $0.75 \%$ per year real rate of wage increase. This represents a decrease of $0.25 \%$ in this assumption.

| Real Rate of Wage Increase Assumption |  |
| :--- | :---: |
| Current | $1.00 \%$ |
| Reasonable Range | $0.50 \%-1.1 \%$ |
| Recommended | $0.75 \%$ |

## Section II: Economic Assumptions

## Payroll Growth Assumption

Background: The assumed future increases in the total payroll of active members is an assumption that only affects the amortization of the unfunded accrued liability and therefore the contribution amounts necessary to fully amortize the unfunded actuarial accrued liability over the specified amortization period. The reasonable range for this assumption is typically between the rates of price inflation and the rate of wage inflation.

The current assumption for the payroll growth assumption is $4.00 \%$ which is the assumed rate of wage inflation over the period ( $3.00 \%$ price inflation plus $1.00 \%$ real rate of wage increases).

Past Experience: Over the past 10 years, the total annual payroll of the System as shown in actuarial valuations has grown at an average annual rate of $3.8 \%$. Over the past two years, the average annual rate of growth is $3.6 \%$.

Recommendation: We recommend we lower this assumption from $4.00 \%$ to $3.75 \%$ to reflect the decrease to the assumed annual rate of wage inflation as presented above.

| Real Rate of Wage Increase Assumption |  |
| :--- | :---: |
| Current | $4.00 \%$ |
| Reasonable Range | $3.00 \%$ to $3.75 \%$ |
| Recommended | $3.75 \%$ |

## Demographic Assumptions

There are several demographic assumptions used in the actuarial valuations performed for the Connecticut State Teachers' Retirement System. They are:

- Rates of Withdrawal
- Rates of Disability
- Rates of Service Retirement
- Rate of Mortality
- Rates of Service Based Salary Increases

The Actuarial Standards Board has issued Actuarial Standard of Practice (ASOP) No. 35, 'Selection of Demographic and Other Noneconomic Assumptions for Measuring Pension Obligations", which provides guidance to actuaries in selecting demographic assumptions for measuring obligations under defined benefit plans. In our opinion, the demographic assumptions recommended in this report have been developed in accordance with ASOP No. 35.

The purpose of a study of demographic experience is to compare what actually happened to the membership during the study period (July 1, 2005 through June 30, 2010) with what was expected to happen based on the assumptions used in the most recent Actuarial Valuations.

Detailed tabulations by age, service and/or gender are performed over the entire study period. The analysis of the experience data focuses on the number of members exposed to each decrement (i.e., retirement, withdrawal, mortality, etc.) and those who experience an event. The raw rates are then established based on this analysis. The raw rates are then compared to the assumed rates. If the actual experience differs significantly from the overall expected results, or if the pattern of actual decrements, or rates of decrement, by age, gender, or service does not follow the expected pattern, new assumptions are recommended. Recommended changes usually do not follow the exact actual experience during the observation period. Judgment is required to extrapolate future experience from past trends and current member behavior. In addition nonrecurring events, such as the impact of recent economic events, need to be taken into account in determining the weight to give to recent experience.

The remainder of this section presents the results of the demographic study. We have prepared tables that show a comparison of the actual and expected decrements and the overall ratio of actual to expected results ( $\mathrm{A} / \mathrm{E}$ Ratios) under the current assumptions. If a change is being proposed, the revised A/E Ratios are shown as well. Salary adjustments, other than the economic assumption for wage inflation discussed in the previous section, are treated as demographic assumptions.

## Rates of Withdrawal

Background: The rates of withdrawal are used to determine the expected number of separations from active service which will occur prior to eligibility for retirement for reasons other than death and disability (e.g., termination of employment). The assumption does not involve the analysis of the election of separating members to receive a refund of eligible funds. There are two separately developed sets of assumed rates for the withdrawal assumption. The first set of rates is the expected rates of withdrawal from active service for each year of service less than 10 years of service. These separating members are entitled to only a full refund of eligible funds. The second set of rates is the expected age-based rates for active members with 10 or more years of service. These separating members are eligible to elect between a full refund of eligible funds or a deferred annuity based upon benefit accrued to date of separation payable as early as age 60 .

## Rates of Withdrawal with Less than 10 Years of Service

Past Experience: For the service based rates (less than 10 years of service), the experience indicates that during the period studied, there were more withdrawals than expected. The following tables provide a comparison of the actual and expected number of withdrawals for members with less than 10 years of service.

| Number of Withdrawals <br> Males with less than 10 years of service |  |  |
| :---: | :---: | :---: |
| Service | Actual Withdrawals | Expected <br> Withdrawals under Current Rates |
| 0 | 156 | 59.5 |
| 1 | 402 | 310.2 |
| 2 | 264 | 189.9 |
| 3 | 252 | 151.7 |
| 4 | 168 | 115.9 |
| 5 | 116 | 81.9 |
| 6 | 110 | 77.8 |
| 7 | 87 | 73.4 |
| 8 | 72 | 67.0 |
| 9 | 51 | 59.4 |
| Total | 1,678 | 1,186.6 |
| Actual to Expe |  | 1.414 |


| Number of Withdrawals <br> Females with less than 10 years of service |  |  |
| :---: | :---: | :---: |
| Service | Actual Withdrawals | Expected <br> Withdrawals under Current Rates |
| 0 | 424 | 146.2 |
| 1 | 1,239 | 1,089.4 |
| 2 | 923 | 790.7 |
| 3 | 755 | 641.1 |
| 4 | 585 | 565.5 |
| 5 | 531 | 498.4 |
| 6 | 443 | 438.5 |
| 7 | 401 | 332.4 |
| 8 | 302 | 264.2 |
| 9 | 237 | 201.6 |
| Total | 5,840 | 4,967.8 |
| Actual to Expe |  | 1.176 |

An actual to expected ratio of greater than 1.00 results from more actual withdrawals than anticipated and would typically generate actuarial gains to the System. The actual rates of withdrawal over the study period are compared with the rates produced in the past two experience studies (current expected and prior expected rates) in the following graphs.



Recommendation: We note that for both males and females, the expected rates have predicted fewer withdrawals than the actual experience for those with less than 5 years of service. These withdrawing members have a very minor liability which is based upon a distribution of all eligible funds. The actual to expected ratio for males with from 5 through 9 years of service was 1.213 and for females with the same service range was 1.103 . The assumption was revised at the time of the last experience study and given the current poor labor market conditions, we are not inclined to increase the future expectation of withdrawal for either gender at this time.

## Rates of Withdrawal with 10 or More Years of Service

Past Experience: For these age based rates for members with at least 10 years of service, the experience indicates that during the period studied there were fewer withdrawals than expected for fully vested members. The following tables provide a comparison of the actual and expected number of withdrawals for members with 10 or more years of service. This table for male rates also includes our recommended change to the age $55-59$ rates.

| Number of Withdrawals <br> Males with 10 or more years of service |  |  |  |
| :---: | :---: | :---: | :---: |
|  | Actual <br> Expected <br> Withdrawals | Withdrawals under <br> Current Rates | Withdrawals under <br> Proposed Rates |
| Age | 6 | 6.6 | 6.6 |
| Under 35 | 31 | 40.0 | 40.0 |
| $35-39$ | 46 | 43.3 | 43.3 |
| $40-44$ | 35 | 50.9 | 50.9 |
| $45-49$ | 48 | 76.0 | 76.0 |
| $50-54$ | 24 | 60.3 | 44.4 |
| $55-59$ | 190 | 277.0 | 261.1 |
| Total |  |  |  |
|  |  | 0.686 | 0.728 |
| Actual to Expected Ratio |  |  |  |


| Number of Withdrawals <br> Females with 10 <br> or more years of service |  |  |
| :---: | :---: | :---: |
|  | Actual <br> Withdrawals | Withdrawals under <br> Current Rates |
|  | 73 | 65.3 |
| Age | 249 | 291.9 |
| Under 35 | 156 | 180.6 |
| $35-39$ | 145 | 137.3 |
| $40-44$ | 134 | 172.6 |
| $45-49$ | 141 | 151.2 |
| $50-54$ | 898 | 998.9 |
| $55-59$ |  | 0.899 |
| Total |  |  |
| Actual to Expected Ratio |  |  |

Since the rates of withdrawal for vested members are much lower than non-vested members, there are not a large number of withdrawals expected or experienced. Again, we do not feel the current experience, as impacted by the significant change to the labor markets and economy, are completely credible for making modification to the current rates. We recommend only a change to the rates for males age 55 to 59 based upon the review of the prior rates set in the two prior experience studies. The actual rates of withdrawal over the study period are compared with the rates produced in the past two experience studies (current expected and prior expected rates) in the following graphs. Our recommended change to the male age $55-59$ rates is also shown.



Recommendation: It is common for rates of withdrawal for vested members to be lower than expected during times of tighter labor markets. It is our opinion that current assumed rates are more credible estimates for the long term future rates of withdrawal than the current experience. We recommend only an adjustment to the rates of males age 55 to 59 in order to partially reflect the current experience and the rates from the prior experience study for this demographic.

## Section III: Demographic Assumptions

## Rates of Disability

Background: The rates of disability are used to anticipate the expected number of separations due to disabilities of eligible active members. As rates of disability are very small, the number of disabilities incurred and expected is small relative to other decrements. When a disability does occur, it will result in an increase in the plan liability to reflect the immediate annuity payable to eligible disabled members at typically earlier ages.

Past Experience: Current experience represents a decline in the rates of disability from the expected rates. In the prior experience study, the prior actuary adjusted rates to better reflect the experience over the 5 year study period ending June 30, 2005. Below we provide the charts of the current actual rates observed, the current expected rates and the rates expected prior to 2005.


## Section III: Demographic Assumptions



Recommendation: The charts show that the current expected rates are a good fit to the age related trend in actual disabilities. The assumption was revised at the time of the last experience study. We recommend no change to the current rates of disability.

## Rates of Retirement

Background: The rates of retirement are used to determine the expected number of separations from active service due to retirement. The plan provides for three types of retirement based on different eligibility requirements. There are three sets of retirement decrements to handle the different types of retirement.

## Rates of Normal Retirement

## Past Experience:

| Number of Retirements <br> Males eligible for normal retirement |  |  |
| :---: | :---: | :---: |
|  | Actual <br> Retirements | Expected <br> Retirements under <br> Current Rates |
| Age | 0 | 0.0 |
| Under 55 | 1 | 0.4 |
| 55 | 12 | 10.8 |
| 56 | 136 | 146.3 |
| 57 | 235 | 254.5 |
| 58 | 233 | 277.2 |
| 59 | 382 | 295.7 |
| 60 | 237 | 239.6 |
| 61 | 183 | 176.8 |
| 62 | 127 | 126.0 |
| 63 | 74 | 85.8 |
| 64 | 59 | 79.2 |
| 65 | 40 | 42.7 |
| 66 | 21 | 28.9 |
| 67 | 24 | 19.6 |
| 68 | 19 | 12.1 |
| 69 | 28 | 106.0 |
| 70 and over | 1,811 | $1,901.5$ |
| Total |  |  |
| Actual\|| to Expected Ratio |  | 0.952 |

Over the past five years, there were 1,811 male actual normal retirements compared to 1,902 predicted by the normal retirement rates for males.

| Number of Retirements <br> Females eligible for normal retirement |  |  |
| :---: | :---: | :---: |
|  | Actual <br> Retirements | Expected <br> Retirements under <br> Current Rates |
| Age | 9 | 1.8 |
| Under 55 | 6 | 2.1 |
| 55 | 31 | 26.1 |
| 56 | 366 | 283.8 |
| 57 | 330 | 345.6 |
| 58 | 295 | 321.3 |
| 59 | 738 | 651.4 |
| 60 | 497 | 553.2 |
| 61 | 378 | 416.9 |
| 62 | 282 | 315.2 |
| 63 | 222 | 236.0 |
| 64 | 226 | 233.7 |
| 65 | 137 | 157.5 |
| 66 | 88 | 107.1 |
| 67 | 62 | 78.0 |
| 68 | 42 | 53.7 |
| 69 | 125 | 228.4 |
| 70 and over | 3,834 | $4,011.8$ |
| Total |  |  |
| Actual to Expected Ratio |  | 0.956 |

Over the past five years, there were 3,834 female actual normal retirements compared with 4,012 predicted by the normal retirement rates for females. As seen in the tables above for both males and females, the current assumed rates continue to be a good estimate of the expectation of normal retirement rates. The following graphs show the actual rates of retirement by age compared with the current assumed retirement rates as well as with the assumed rates prior to the 2005 study. On the following graphs, please note the large discrepancies in the rates at the early ages are based on very small amounts of exposure (not many members were eligible but a majority of them did retire). In other words, this small group is very visible on the graphs but has little overall impact.

## Section III: Demographic Assumptions




Recommendation: The overall actual to expected ratio is well within the reasonable range and the current assumption remains a good estimate of future expectation. We recommend no change to the current rates of normal retirement for males or females.

## Rates of Proratable Retirement

Past Experience:

| Number of Retirements <br> Males eligible for proratable retirement |  |  |
| :---: | :---: | :---: |
| Age | Actual Retirements | Expected <br> Retirements under Current Rates |
| 60 | 16 | 13.3 |
| 61 | 9 | 10.6 |
| 62 | 12 | 21.6 |
| 63 | 7 | 10.9 |
| 64 | 10 | 7.5 |
| 65 | 8 | 10.8 |
| 66 | 7 | 9.8 |
| 67 | 3 | 6.2 |
| 68 | 5 | 4.6 |
| 69 | 3 | 5.6 |
| 70 and over | 5 | 7.9 |
| Total | 85 | 108.8 |
| Actual to Expecte |  | 0.781 |


| Number of Retirements <br> Females eligible for proratable retirement |  |  |
| :---: | :---: | :---: |
| Age | Actual Retirements | Expected Retirements under Current Rates |
| 60 | 64 | 62.5 |
| 61 | 52 | 64.3 |
| 62 | 45 | 63.3 |
| 63 | 33 | 33.9 |
| 64 | 26 | 21.9 |
| 65 | 28 | 29.8 |
| 66 | 12 | 15.8 |
| 67 | 14 | 14.4 |
| 68 | 9 | 7.3 |
| 69 | 4 | 5.2 |
| 70 and over | 16 | 15.9 |
| Total | 303 | 334.3 |
| Actual to Expect |  | 0.906 |

Over the five year period, there were 85 male proratable retirements compared with 109 expected. There were 303 female proratable retirements compared with 334 expected. The following graphs show the actual rates of proratable retirement based on age compared with the current assumed rates of retirement as well as with the assumed rates prior to the five year study period. The current period represents a departure from the experience of the prior 10 years and is impacted by the more recent and shorter term economic downturn. The following charts show the current actual rates along with the current expected rates and the rates expected prior to the 2005 study.

## Section III: Demographic Assumptions




Recommendation: The current experience does not provide compelling evidence to adjust the expected rates of proratable retirement. We do not recommend a change to the proratable retirement assumptions for males or females.

## Rates of Early Retirement

Past Experience: The following tables provide the actual and expected counts of early retirements and include expected counts under the proposed change to the assumption.

| Age | Number of Retirements <br> Males eligible for early retirement |  | Expected <br> Retirements under Proposed Rates |
| :---: | :---: | :---: | :---: |
|  | Actual <br> Retirements | Expected <br> Retirements under Current Rates |  |
| Under 50 | 2 | 18.1 | 9.1 |
| 50 | 1 | 7.4 | 7.4 |
| 51 | 5 | 9.9 | 9.9 |
| 52 | 7 | 18.3 | 15.3 |
| 53 | 17 | 23.6 | 23.6 |
| 54 | 29 | 49.4 | 39.5 |
| 55 | 50 | 69.8 | 62.8 |
| 56 | 77 | 110.7 | 94.9 |
| 57 | 94 | 136.6 | 122.9 |
| 58 | 88 | 123.0 | 111.8 |
| 59 | 83 | 106.7 | 97.8 |
| Total | 453 | 673.4 | 595.0 |
| Actual to Expected Ratio |  | 0.673 | 0.761 |


| Age | Number of Retirements Females eligible for early retirement |  | Expected <br> Retirements under Proposed Rates |
| :---: | :---: | :---: | :---: |
|  | Actual <br> Retirements | Expected <br> Retirements under Current Rates |  |
| Under 50 | 5 | 54.2 | 27.1 |
| 50 | 4 | 20.9 | 20.9 |
| 51 | 11 | 27.7 | 27.7 |
| 52 | 30 | 67.9 | 50.9 |
| 53 | 45 | 97.7 | 76.0 |
| 54 | 61 | 140.0 | 101.8 |
| 55 | 156 | 283.3 | 226.7 |
| 56 | 217 | 340.2 | 280.1 |
| 57 | 167 | 315.9 | 249.4 |
| 58 | 168 | 288.3 | 230.6 |
| 59 | 181 | 260.9 | 221.8 |
| Total | 1,045 | 1,896.9 | 1,513.0 |
| Actual to Expec |  | 0.551 | 0.691 |

There were 453 actual male early retirements compared with 673 predicted by the early retirement assumptions. There were 1,045 female early retirements compared with 1,897 predicted by the early retirement assumptions. The following graphs show the actual rates of early retirement based on age compared with the current early retirement assumptions as well as with the assumptions prior to the 2005 study. Our recommended rates are also included.



Recommendation: The assumed rates of early retirement were increased at the time of the last experience study but the actual number of early retirements has decreased from the prior study period. We recommend decreasing the assumed early retirement rates for both males and females to better recognize the recent decline in early retirements. As will be noted, our recommended rates only partially reflect the recent experience and maintain a sufficient margin above the current experience to address the longer term historic trend of higher earlier retirement rates.

## Rates of Mortality

Background: Assumed rates of post-retirement mortality are very important assumptions for the actuarial valuation because they predict life expectancies and therefore, the duration of pension payments. As life expectancies are expected to continue to increase in the future, mortality rates are sometimes projected by actuaries to anticipate expected mortality improvements. The current mortality rates are projected to 2019.

Rates of Healthy Post-Retirement Mortality
Past Experience:

| Number of Deaths <br> Service Retirements and Beneficiaries <br> Males |  |  |
| :---: | :---: | :---: |
|  | Actual Deaths <br> Expected Deaths <br> under Current <br> Rates |  |
| Age | 7 | 0.2 |
| $50-54$ | 22 | 8.2 |
| $55-59$ | 87 | 62.4 |
| $60-64$ | 97 | 103.5 |
| $65-69$ | 178 | 144.6 |
| $70-74$ | 261 | 219.1 |
| $75-79$ | 262 | 256.2 |
| $80-84$ | 187 | 197.8 |
| $85-89$ | 104 | 90.6 |
| $90-94$ | 24 | 22.0 |
| $95-99$ | 6 | 10.3 |
| 100 and over | 1,235 | $1,115.0$ |
| Total |  | 1.108 |
| Actual to Expected Ratio |  |  |


| Number of Deaths <br> Service Retirements and Beneficiaries <br> Females |  |  |
| :---: | :---: | :---: |
|  |  |  |
| Age | Actual Deaths | Expected Deaths under Current Rates |
| 50-54 | 21 | 0.5 |
| 55-59 | 48 | 16.9 |
| 60-64 | 110 | 92.5 |
| 65-69 | 106 | 150.0 |
| 70-74 | 166 | 207.1 |
| 75-79 | 310 | 295.7 |
| 80-84 | 379 | 336.5 |
| 85-89 | 409 | 367.2 |
| 90-94 | 394 | 325.7 |
| 95-99 | 226 | 164.3 |
| 100 and over | 44 | 36.4 |
| Total | 2,213 | 1,992.7 |
| Actual to Expecte |  | 1.111 |

Because the current assumed rates of mortality for both males and females anticipate future mortality improvements, we would expect actual deaths during the study period to be somewhat greater than expected deaths which is the case. The graphs below show a comparison of the previous, present, and actual rates of post-retirement deaths.



Recommendation: The experience for post-retirement mortality indicates that overall approximately $11 \%$ more members have died than expected during the study period which has resulted in modest gains to the system. The assumption currently in use is the RP-2000 Combined Mortality Table projected 19 years using scale AA, with a two year setback for males and females. (A two year "set back" means that the tabular rates for a 60 year old would be applied as the mortality rate for a 62 year old.) We recommend no change to the post-retirement mortality assumption.

## Rates of Disability Mortality

Past Experience: There were 22 deaths of male disabled members compared with 5.8 expected over the study period. There were 83 female disabled deaths compare with 17.9 expected over the study period. Since there are not a large number of disabled members in the data, the experience observed is not statistically significant for assessing mortality rates.

| Number of Deaths Disabled Members Males |  |  |
| :---: | :---: | :---: |
| Age | Actual Deaths | Expected Deaths under Current Rates |
| 50-54 | 3 | 0.4 |
| 55-59 | 11 | 2.3 |
| 60-64 | 5 | 0.7 |
| 65-69 | 0 | 0.6 |
| 70-74 | 2 | 1.3 |
| 75-79 | 0 | 0.2 |
| 80-84 | 1 | 0.3 |
| 85-89 | 0 | 0.0 |
| 90-94 | 0 | 0.0 |
| 95-99 | 0 | 0.0 |
| 100 and over | 0 | 0.0 |
| Total | 22 | 5.8 |
| Actual to Expected |  | 3.806 |


|  | Number of Deaths <br> Disabled Members <br> Females | Agpected Deaths <br> under Current <br> Rates |
| :---: | :---: | :---: |
| Age | Actual Deaths | 1.1 |
| $50-54$ | 4 | 5.7 |
| $55-59$ | 44 | 1.7 |
| $60-64$ | 17 | 0.5 |
| $65-69$ | 2 | 1.1 |
| $70-74$ | 4 | 0.3 |
| $75-79$ | 1 | 0.8 |
| $80-84$ | 1 | 2.1 |
| $85-89$ | 1 | 3.5 |
| $90-94$ | 6 | 0.8 |
| $95-99$ | 2 | 0.3 |
| 100 and over | 1 | 17.9 |
| Total | 83 | 4.637 |

Recommendation: The current mortality assumption for disabled members is the mortality assumption for healthy retired members set forward 10 years. This assumption has a large degree of conservatism but does not materially affect the valuation results due to the small number of disabled retirees compared to service retirees. We recommend no change to the current assumption at this time.

## Rates of Pre-Retirement Mortality

Recommendation: Again, due to the very limited number of active member deaths, we recommend the active mortality assumption continue to be the same mortality assumption as for retirees and beneficiaries and continue to reduce the rates at each age by $25 \%$. This continues to provide sufficient margin in expected rates of death of active members. As with disability benefits, active member death benefits are ancillary to retirement benefits and therefore, the experience of active member mortality does not materially affect valuation results.

## Rates of Service Based Salary Increases

Background: The assumed rates of salary increase provide the expected growth in future salaries both for approximating the future benefits to be provided and the future amounts expected to be contributed to the System through normal cost contributions of members and the employer. Therefore, this assumption is very material to valuation results. The actuarial standards of practice recommend a "building block" approach to developing this assumption. Under this approach, the assumption is composed of an assumption for wage inflation (the "across the board" increases of active salaries), and an assumed salary increase scale based on the years of service.

The first step in developing the service based rates of increase is to subtract the apparent wage inflation component from the actual salary rates of increase as measured over the study period. The average annual rate of inflation over the five-year period ending June 30, 2010 was $2.30 \%$ and the apparent real rate of wage inflation (wage increases above price inflation or CPI) in the data was $0.82 \%$. The sum of these components equals an apparent annual rate of wage inflation of $3.12 \%$ over the five year period. The apparent rate of wage inflation is first removed from the actual rates of salary increase and the remaining rates reflect the apparent service based increases in salaries due to step increases, promotions, and educational increases. Next, we assess the current assumed rates of service based salary increases and recommend adjustments where necessary.

Again, the focus of this assumption is the long-term expectation and should not be significantly affected by short-term fluctuations. The actuary then combines the wage inflation assumption with the assumed rates of service based increases to produce the rates of assumed salary increases based upon years of service.

Past Experience: Total salary increases averaged $5.7 \%$ per year compared with $5.4 \%$ expected increases in salaries over the five year period. We note that the latest year of the salary experience clearly shows the most recent trend is declining rates of growth. This trend is also apparent in the latest collective bargaining agreements that we reviewed which provide additional information on the short-term future expectation of salary increases.

We note the following in review of the past experience:

1. Wage Inflation or the "across the board" rate of increase is consistently lower than the $4.0 \%$ assumed rate of increase.
2. Rates of service based increases appear more level over the first 10 -years than the current assumed rates.

## Section III: Demographic Assumptions



In the graph above, the lower than assumed wage inflation component of the salary increases is shown as the difference between the expected rates (red line) and the actual rates experienced (blue line) beginning around 20 years of service and beyond.

In the following table, we provide our analysis under the building block approach for the development of the rates of service based increases.

| Years of Service | Actual Rate of Salary Increase | Apparent Service Based Increases (Actual Rate Less Apparent Wage Inflation of 3.12\% ) | Current Service Based Increase Assumption | Proposed Service <br> Based Increase Assumption |
| :---: | :---: | :---: | :---: | :---: |
| 1 | 10.79\% | 7.67\% | 3.50\% | 3.25\% |
| 2 | 7.24\% | 4.12\% | 3.50\% | 3.25\% |
| 3 | 6.98\% | 3.86\% | 3.50\% | 3.25\% |
| 4 | 7.17\% | 4.05\% | 3.50\% | 3.25\% |
| 5 | 7.18\% | 4.06\% | 2.50\% | 3.25\% |
| 6 | 7.46\% | 4.34\% | 2.50\% | 3.25\% |
| 7 | 7.41\% | 4.29\% | 2.50\% | 3.25\% |
| 8 | 7.38\% | 4.26\% | 2.50\% | 3.25\% |
| 9 | 7.63\% | 4.51\% | 2.50\% | 3.25\% |
| 10 | 7.04\% | 3.92\% | 1.50\% | 1.75\% |
| 11 | 6.70\% | 3.58\% | 1.50\% | 1.75\% |
| 12 | 6.38\% | 3.26\% | 1.50\% | 1.75\% |
| 13 | 5.65\% | 2.53\% | 1.50\% | 1.75\% |
| 14 | 5.25\% | 2.13\% | 1.50\% | 1.75\% |
| 15 | 4.78\% | 1.66\% | 0.00\% | 0.25\% |
| 16 | 4.16\% | 1.04\% | 0.00\% | 0.25\% |
| 17 | 3.86\% | 0.74\% | 0.00\% | 0.25\% |
| 18 | 3.70\% | 0.58\% | 0.00\% | 0.25\% |
| 19 | 3.58\% | 0.46\% | 0.00\% | 0.25\% |
| 20 | 3.68\% | 0.56\% | 0.00\% | 0.00\% |
| 21 | 3.48\% | 0.36\% | 0.00\% | 0.00\% |
| 22 | 3.38\% | 0.26\% | 0.00\% | 0.00\% |
| 23 | 3.27\% | 0.15\% | 0.00\% | 0.00\% |
| 24 | 3.39\% | 0.27\% | 0.00\% | 0.00\% |
| 25+ | 3.21\% | 0.09\% | 0.00\% | 0.00\% |

Recommendation (Long-Term): Based upon our analysis, we have recommended a $0.25 \%$ reduction in the wage inflation assumption from $4.00 \%$ to $3.75 \%$ as discussed previously in the economic assumptions. We also recommend adjustments to the assumed service based increases as provided in the table above.

Recommendation (Short-Term): In reviewing the more recent trend in the rates of salary increases along with several collective bargaining agreements, we recommend an alternate assumption for salary increases occurring from 2010 through 2012. The short-term recommendation represents a $0.50 \%$ reduction in the rates of increase for 1 to 9 years of service and a $0.25 \%$ reduction in the rates of increase for after 20 years of service.

Combining our assumption for rates of service based increases (long and short term) with the recommended wage inflation assumption produces the following table of service related salary increase rates. The table also provides a comparison of our recommendations with the current assumption.

|  | Current Salary <br> Increase | Proposed Long <br> Term Salary <br> Increase | Proposed Short <br> Term Salary <br> Increase |
| :---: | :---: | :---: | :---: |
| Years of Service | Assumption | Assumption | Assumption |$|$| $1-4$ | $7.50 \%$ | $7.00 \%$ | $6.50 \%$ |
| :---: | :---: | :---: | :---: |
| $5-9$ | $6.50 \%$ | $7.00 \%$ | $5.50 \%$ |
| $10-14$ | $5.50 \%$ | $5.50 \%$ | $4.00 \%$ |
| $15-19$ | $4.00 \%$ | $4.00 \%$ | $3.50 \%$ |
| $20-24$ | $4.00 \%$ | $3.75 \%$ | $3.50 \%$ |
| $25+$ | $4.00 \%$ | $3.75 \%$ |  |

The following chart compares the most recent year of salary experience with our long and short term recommended assumptions.


## Section III: Demographic Assumptions

## Other Actuarial Assumptions

Percent Married: Currently $85 \%$ of active male members and $75 \%$ of active female members are assumed to be married with the male spouse three years older than the female spouse. This is a common and reasonable assumption and we recommend maintaining this assumption.

Actuarial Cost Method: The cost method is used to allocate the present value of benefits between past service (actuarial accrued liability) and future service (normal cost). Currently the valuation uses the entry age normal actuarial cost method. This is the most widely used cost method of large public sector plans and has demonstrated the highest degree of stability as compared to alternative methods. We recommend no change to the use of this method.

Actuarial Value of Assets (Smoothing): The purpose of asset smoothing is to dampen the impact that market volatility has on valuation results by spreading the unexpected market gains and losses over several years. Currently, the System uses a four-year actuarial smoothing method. In each valuation, the actuarial value of assets is determined by adjusting the expected actuarial value by $25 \%$ of the difference between the actual and expected market value of assets measured in each of the current and three prior years. The current method meets with all applicable actuarial and accounting standards.

Most large retirement systems utilize a smoothing method in determining the value of assets for valuation purposes with a five-year smoothing period being the most common and four-year smoothing being the second most common. In consideration of the recent market performance, a longer smoothing period would reduce the amount of the investment losses recognized in each year but also would be slower to recognize the gains of the markets as they recover. The real impact over time to the funding of the plan will be significantly affected by the long-term investment returns experienced compared to the return assumption and not the length of the asset smoothing period. We do not recommend a change to a longer smoothing period that is applied retroactively. A change to a longer smoothing period applied prospectively would be expected to slow down the recognition of gains experienced as the markets recover and could be expected to increase required funding in future valuations.

Amortization Method: The unfunded actuarial accrued liability (liability in excess of assets) is amortized using a level percentage of payroll method over the amortization periods prescribed by statute. The payroll growth assumption is used to determine the percentage of payroll required over the remaining amortization period to fully amortize the unfunded liability. In this study, we recommend a decrease to the annual payroll growth rate from $4.00 \%$ to $3.75 \%$ which is consistent with our recommendation for the long-term expected rate of wage inflation. It is our understanding that the length of the amortization period is defined by statute and is not within the Board's authority to change.

TABLE 1 - RATES OF WITHDRAWAL FROM ACTIVE SERVICE

| Less than 10 years of service |  |  | 10 or more years of service |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Years of Service | Male | Female | Age | Male | Female |
| 0 | 0.140 | 0.120 | 25 | 0.0120 | 0.0350 |
| 1 | 0.085 | 0.090 | 26 | 0.0120 | 0.0350 |
| 2 | 0.055 | 0.070 | 27 | 0.0120 | 0.0350 |
| 3 | 0.045 | 0.060 | 28 | 0.0120 | 0.0350 |
| 4 | 0.035 | 0.055 | 29 | 0.0120 | 0.0350 |
| 5 | 0.025 | 0.050 | 30 | 0.0120 | 0.0350 |
| 6 | 0.024 | 0.045 | 31 | 0.0120 | 0.0350 |
| 7 | 0.023 | 0.035 | 32 | 0.0120 | 0.0350 |
| 8 | 0.022 | 0.030 | 33 | 0.0120 | 0.0350 |
| 9 | 0.021 | 0.025 | 34 | 0.0120 | 0.0350 |
|  |  |  | 35 | 0.0120 | 0.0350 |
|  |  |  | 36 | 0.0120 | 0.0350 |
|  |  |  | 37 | 0.0120 | 0.0350 |
|  |  |  | 38 | 0.0120 | 0.0310 |
|  |  |  | 39 | 0.0120 | 0.0270 |
|  |  |  | 40 | 0.0120 | 0.0230 |
|  |  |  | 41 | 0.0120 | 0.0190 |
|  |  |  | 42 | 0.0120 | 0.0160 |
|  |  |  | 43 | 0.0122 | 0.0150 |
|  |  |  | 44 | 0.0124 | 0.0140 |
|  |  |  | 45 | 0.0126 | 0.0130 |
|  |  |  | 46 | 0.0128 | 0.0120 |
|  |  |  | 47 | 0.0130 | 0.0110 |
|  |  |  | 48 | 0.0152 | 0.0115 |
|  |  |  | 49 | 0.0174 | 0.0120 |
|  |  |  | 50 | 0.0196 | 0.0125 |
|  |  |  | 51 | 0.0218 | 0.0130 |
|  |  |  | 52 | 0.0240 | 0.0130 |
|  |  |  | 53 | 0.0252 | 0.0140 |
|  |  |  | 54 | 0.0264 | 0.0150 |
|  |  |  | 55 | 0.0276 | 0.0160 |
|  |  |  | 56 | 0.0288 | 0.0170 |
|  |  |  | 57 | 0.0300 | 0.0180 |
|  |  |  | 58 | 0.0300 | 0.0180 |
|  |  |  | 59 | 0.0300 | 0.0190 |

TABLE 2 - RATES OF DISABILITY WHILE IN ACTIVE SERVICE

| Age | Male | Female |
| :---: | :---: | :---: |
| 20 | 0.000455 | 0.00050 |
| 21 | 0.000455 | 0.00050 |
| 22 | 0.000455 | 0.00050 |
| 23 | 0.000455 | 0.00050 |
| 24 | 0.000455 | 0.00050 |
| 25 | 0.000455 | 0.00050 |
| 26 | 0.000455 | 0.00050 |
| 27 | 0.000455 | 0.00050 |
| 28 | 0.000455 | 0.00047 |
| 29 | 0.000455 | 0.00044 |
| 30 | 0.000455 | 0.00041 |
| 31 | 0.000455 | 0.00038 |
| 32 | 0.000455 | 0.00035 |
| 33 | 0.000455 | 0.00037 |
| 34 | 0.000455 | 0.00039 |
| 35 | 0.000455 | 0.00041 |
| 36 | 0.000455 | 0.00043 |
| 37 | 0.000455 | 0.00045 |
| 38 | 0.000520 | 0.00054 |
| 39 | 0.000650 | 0.00063 |
| 40 | 0.000715 | 0.00072 |
| 41 | 0.000845 | 0.00081 |
| 42 | 0.001040 | 0.00090 |
| 43 | 0.00170 | 0.00100 |
| 44 | 0.001430 | 0.00110 |
| 45 | 0.001625 | 0.00120 |
| 46 | 0.001820 | 0.00130 |
| 47 | 0.002015 | 0.00140 |
| 48 | 0.002340 | 0.00181 |
| 49 | 0.002730 | 0.00222 |
| 50 | 0.003250 | 0.00263 |
| 51 | 0.003900 | 0.00304 |
| 52 | 0.004615 | 0.00345 |
| 53 | 0.005330 | 0.00376 |
| 54 | 0.006175 | 0.00407 |
| 55 | 0.007150 | 0.00438 |
| 56 | 0.008320 | 0.00469 |
| 57 | 0.009490 | 0.00500 |
|  | 0.010790 | 0.00500 |
| 3 | 0.012805 | 0.00500 |
| 3 | 0.00500 |  |

TABLE 3 - RATES OF RETIREMENT FROM ACTIVE SERVICE

| Age | Normal |  | Proratable |  | Early |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Male | Female | Male | Female | Male | Female |
| 50 | 0.275 | 0.150 |  |  | 0.020 | 0.020 |
| 51 | 0.275 | 0.150 |  |  | 0.020 | 0.020 |
| 52 | 0.275 | 0.150 |  |  | 0.025 | 0.030 |
| 53 | 0.275 | 0.150 |  |  | 0.030 | 0.035 |
| 54 | 0.275 | 0.150 |  |  | 0.040 | 0.040 |
| 55 | 0.385 | 0.300 |  |  | 0.045 | 0.060 |
| 56 | 0.385 | 0.300 |  |  | 0.060 | 0.070 |
| 57 | 0.385 | 0.300 |  |  | 0.090 | 0.075 |
| 58 | 0.385 | 0.300 |  |  | 0.100 | 0.080 |
| 59 | 0.385 | 0.300 |  |  | 0.110 | 0.085 |
| 60 | 0.220 | 0.200 | 0.060 | 0.054 |  |  |
| 61 | 0.253 | 0.225 | 0.060 | 0.072 |  |  |
| 62 | 0.253 | 0.225 | 0.150 | 0.099 |  |  |
| 63 | 0.275 | 0.225 | 0.100 | 0.072 |  |  |
| 64 | 0.275 | 0.225 | 0.100 | 0.072 |  |  |
| 65 | 0.363 | 0.300 | 0.200 | 0.135 |  |  |
| 66 | 0.275 | 0.300 | 0.200 | 0.108 |  |  |
| 67 | 0.275 | 0.300 | 0.200 | 0.135 |  |  |
| 68 | 0.275 | 0.300 | 0.200 | 0.108 |  |  |
| 69 | 0.275 | 0.300 | 0.350 | 0.108 |  |  |
| 70 | 1.000 | 0.400 | 0.350 | 0.108 |  |  |
| 71 | 1.000 | 0.400 | 0.350 | 0.108 |  |  |
| 72 | 1.000 | 0.400 | 0.350 | 0.108 |  |  |
| 73 | 1.000 | 0.400 | 0.350 | 0.108 |  |  |
| 74 | 1.000 | 0.400 | 0.350 | 0.180 |  |  |
| 75 | 1.000 | 0.400 | 0.400 | 0.180 |  |  |
| 76 | 1.000 | 0.400 | 0.400 | 0.180 |  |  |
| 77 | 1.000 | 0.400 | 0.400 | 0.180 |  |  |
| 78 | 1.000 | 0.400 | 0.400 | 0.180 |  |  |
| 79 | 1.000 | 0.400 | 0.400 | 0.180 |  |  |
| 80 | 1.000 | 1.000 | 1.000 | 1.000 |  |  |

TABLE 4 - RATES OF MORTALITY WHILE IN ACTIVE SERVICE

| Age | Male | Female |
| :---: | :---: | :---: |
| 20 | 0.000164 | 0.000108 |
| 21 | 0.000173 | 0.000107 |
| 22 | 0.000180 | 0.000106 |
| 23 | 0.000190 | 0.000104 |
| 24 | 0.000198 | 0.000105 |
| 25 | 0.000210 | 0.000109 |
| 26 | 0.000220 | 0.000113 |
| 27 | 0.000233 | 0.000119 |
| 28 | 0.000253 | 0.000128 |
| 29 | 0.000260 | 0.000133 |
| 30 | 0.000268 | 0.000140 |
| 31 | 0.000281 | 0.000148 |
| 32 | 0.000303 | 0.000164 |
| 33 | 0.000341 | 0.000198 |
| 34 | 0.000383 | 0.000225 |
| 35 | 0.000431 | 0.000249 |
| 36 | 0.000479 | 0.000269 |
| 37 | 0.000527 | 0.000289 |
| 38 | 0.000574 | 0.000307 |
| 39 | 0.000617 | 0.000324 |
| 40 | 0.000645 | 0.000343 |
| 41 | 0.000670 | 0.000365 |
| 42 | 0.000695 | 0.000397 |
| 43 | 0.000721 | 0.000436 |
| 44 | 0.000753 | 0.000479 |
| 45 | 0.000790 | 0.000527 |
| 46 | 0.000833 | 0.000579 |
| 47 | 0.000882 | 0.000620 |
| 48 | 0.000927 | 0.000662 |
| 49 | 0.000976 | 0.000704 |
| 50 | 0.001027 | 0.000761 |
| 51 | 0.001080 | 0.000824 |
| 52 | 0.001136 | 0.000907 |
| 53 | 0.001276 | 0.001022 |
| 54 | 0.001363 | 0.001158 |
| 55 | 0.001490 | 0.001316 |
| 56 | 0.001633 | 0.001502 |
| 57 | 0.001888 | 0.001749 |
| 58 | 0.002231 | 0.002067 |
| 59 | 0.002541 | 0.002372 |
| 60 | 0.002911 | 0.002675 |
| 61 | 0.003282 | 0.003029 |
| 62 | 0.003725 | 0.003447 |
| 63 | 0.004320 | 0.003965 |
| 64 | 0.004928 | 0.004539 |
| 65 | 0.005744 | 0.005215 |
| 66 | 0.006472 | 0.005877 |
| 67 | 0.007308 | 0.006618 |
| 68 | 0.008428 | 0.007469 |
| 69 | 0.009403 | 0.008294 |
| 70 | 0.010253 | 0.009168 |

TABLE 5 - RATES OF MORTALITY FOR RETIRED MEMBERS AND BENEFICIARIES

| Age | Male | Female | Age | Male | Female |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 20 | 0.000219 | 0.000144 | 71 | 0.015149 | 0.013510 |
| 21 | 0.000230 | 0.000143 | 72 | 0.016663 | 0.015221 |
| 22 | 0.000240 | 0.000141 | 73 | 0.018437 | 0.016572 |
| 23 | 0.000253 | 0.000139 | 74 | 0.020471 | 0.018432 |
| 24 | 0.000264 | 0.000140 | 75 | 0.022802 | 0.020100 |
| 25 | 0.000280 | 0.000145 | 76 | 0.025438 | 0.022277 |
| 26 | 0.000293 | 0.000151 | 77 | 0.028943 | 0.024128 |
| 27 | 0.000311 | 0.000158 | 78 | 0.032259 | 0.026583 |
| 28 | 0.000337 | 0.000170 | 79 | 0.036581 | 0.029844 |
| 29 | 0.000347 | 0.000177 | 80 | 0.041439 | 0.032898 |
| 30 | 0.000357 | 0.000187 | 81 | 0.046947 | 0.036320 |
| 31 | 0.000375 | 0.000197 | 82 | 0.053179 | 0.040147 |
| 32 | 0.000404 | 0.000218 | 83 | 0.060671 | 0.044435 |
| 33 | 0.000454 | 0.000264 | 84 | 0.069094 | 0.049260 |
| 34 | 0.000511 | 0.000300 | 85 | 0.077020 | 0.054696 |
| 35 | 0.000574 | 0.000332 | 86 | 0.087312 | 0.060831 |
| 36 | 0.000638 | 0.000359 | 87 | 0.096919 | 0.069078 |
| 37 | 0.000703 | 0.000385 | 88 | 0.107454 | 0.078529 |
| 38 | 0.000765 | 0.000409 | 89 | 0.121344 | 0.089273 |
| 39 | 0.000822 | 0.000432 | 90 | 0.136910 | 0.099435 |
| 40 | 0.000860 | 0.000457 | 91 | 0.151302 | 0.112543 |
| 41 | 0.000893 | 0.000486 | 92 | 0.169960 | 0.124375 |
| 42 | 0.000926 | 0.000530 | 93 | 0.185121 | 0.136580 |
| 43 | 0.000962 | 0.000581 | 94 | 0.204586 | 0.148872 |
| 44 | 0.001004 | 0.000639 | 95 | 0.220697 | 0.164072 |
| 45 | 0.001053 | 0.000703 | 96 | 0.236783 | 0.175976 |
| 46 | 0.001111 | 0.000772 | 97 | 0.257507 | 0.187249 |
| 47 | 0.001176 | 0.000827 | 98 | 0.273309 | 0.197713 |
| 48 | 0.001236 | 0.000883 | 99 | 0.288660 | 0.211187 |
| 49 | 0.001301 | 0.000939 | 100 | 0.309359 | 0.219730 |
| 50 | 0.001369 | 0.001015 | 101 | 0.323989 | 0.227030 |
| 51 | 0.001440 | 0.001098 | 102 | 0.338068 | 0.232996 |
| 52 | 0.001514 | 0.001210 | 103 | 0.358628 | 0.244834 |
| 53 | 0.001701 | 0.001363 | 104 | 0.371685 | 0.254498 |
| 54 | 0.001817 | 0.001544 | 105 | 0.383040 | 0.266044 |
| 55 | 0.001986 | 0.001755 | 106 | 0.392003 | 0.279055 |
| 56 | 0.002177 | 0.002003 | 107 | 0.397886 | 0.293116 |
| 57 | 0.002517 | 0.002332 | 108 | 0.400000 | 0.307811 |
| 58 | 0.002974 | 0.002756 | 109 | 0.400000 | 0.322725 |
| 59 | 0.003388 | 0.003162 | 110 | 0.400000 | 0.337441 |
| 60 | 0.003881 | 0.003567 | 111 | 0.400000 | 0.351544 |
| 61 | 0.004376 | 0.004038 | 112 | 0.400000 | 0.364617 |
| 62 | 0.004966 | 0.004596 | 113 | 0.400000 | 0.376246 |
| 63 | 0.005760 | 0.005286 | 114 | 0.400000 | 0.386015 |
| 64 | 0.006571 | 0.006052 | 115 | 0.400000 | 0.393507 |
| 65 | 0.007659 | 0.006953 | 116 | 0.400000 | 0.398308 |
| 66 | 0.008629 | 0.007836 | 117 | 0.400000 | 0.400000 |
| 67 | 0.009744 | 0.008824 | 118 | 0.400000 | 0.400000 |
| 68 | 0.011237 | 0.009959 | 119 | 0.400000 | 0.400000 |
| 69 | 0.012537 | 0.011058 | 120+ | 1.000000 | 1.000000 |
| 70 | 0.013671 | 0.012224 |  |  |  |

TABLE 6 - RATES OF MORTALITY FOR DISABILITY MEMBERS

| Age | Male | Female | Age | Male | Female |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 25 | 0.000574 | 0.000332 | 68 | 0.032259 | 0.026583 |
| 26 | 0.000638 | 0.000359 | 69 | 0.036581 | 0.029844 |
| 27 | 0.000703 | 0.000385 | 70 | 0.041439 | 0.032898 |
| 28 | 0.000765 | 0.000409 | 71 | 0.046947 | 0.036320 |
| 29 | 0.000822 | 0.000432 | 72 | 0.053179 | 0.040147 |
| 30 | 0.000860 | 0.000457 | 73 | 0.060671 | 0.044435 |
| 31 | 0.000893 | 0.000486 | 74 | 0.069094 | 0.049260 |
| 32 | 0.000926 | 0.000530 | 75 | 0.077020 | 0.054696 |
| 33 | 0.000962 | 0.000581 | 76 | 0.087312 | 0.060831 |
| 34 | 0.001004 | 0.000639 | 77 | 0.096919 | 0.069078 |
| 35 | 0.001053 | 0.000703 | 78 | 0.107454 | 0.078529 |
| 36 | 0.001111 | 0.000772 | 79 | 0.121344 | 0.089273 |
| 37 | 0.001176 | 0.000827 | 80 | 0.136910 | 0.099435 |
| 38 | 0.001236 | 0.000883 | 81 | 0.151302 | 0.112543 |
| 39 | 0.001301 | 0.000939 | 82 | 0.169960 | 0.124375 |
| 40 | 0.001369 | 0.001015 | 83 | 0.185121 | 0.136580 |
| 41 | 0.001440 | 0.001098 | 84 | 0.204586 | 0.148872 |
| 42 | 0.001514 | 0.001210 | 85 | 0.220697 | 0.164072 |
| 43 | 0.001701 | 0.001363 | 86 | 0.236783 | 0.175976 |
| 44 | 0.001817 | 0.001544 | 87 | 0.257507 | 0.187249 |
| 45 | 0.001986 | 0.001755 | 88 | 0.273309 | 0.197713 |
| 46 | 0.002177 | 0.002003 | 89 | 0.288660 | 0.211187 |
| 47 | 0.002517 | 0.002332 | 90 | 0.309359 | 0.219730 |
| 48 | 0.002974 | 0.002756 | 91 | 0.323989 | 0.227030 |
| 49 | 0.003388 | 0.003162 | 92 | 0.338068 | 0.232996 |
| 50 | 0.003881 | 0.003567 | 93 | 0.358628 | 0.244834 |
| 51 | 0.004376 | 0.004038 | 94 | 0.371685 | 0.254498 |
| 52 | 0.004966 | 0.004596 | 95 | 0.383040 | 0.266044 |
| 53 | 0.005760 | 0.005286 | 96 | 0.392003 | 0.279055 |
| 54 | 0.006571 | 0.006052 | 97 | 0.397886 | 0.293116 |
| 55 | 0.007659 | 0.006953 | 98 | 0.400000 | 0.307811 |
| 56 | 0.008629 | 0.007836 | 99 | 0.400000 | 0.322725 |
| 57 | 0.009744 | 0.008824 | 100 | 0.400000 | 0.337441 |
| 58 | 0.011237 | 0.009959 | 101 | 0.400000 | 0.351544 |
| 59 | 0.012537 | 0.011058 | 102 | 0.400000 | 0.364617 |
| 60 | 0.013671 | 0.012224 | 103 | 0.400000 | 0.376246 |
| 61 | 0.015149 | 0.013510 | 104 | 0.400000 | 0.386015 |
| 62 | 0.016663 | 0.015221 | 105 | 0.400000 | 0.393507 |
| 63 | 0.018437 | 0.016572 | 106 | 0.400000 | 0.398308 |
| 64 | 0.020471 | 0.018432 | 107 | 0.400000 | 0.400000 |
| 65 | 0.022802 | 0.020100 | 108 | 0.400000 | 0.400000 |
| 66 | 0.025438 | 0.022277 | 109 | 0.400000 | 0.400000 |
| 67 | 0.028943 | 0.024128 | 110 | 1.000000 | 1.000000 |

TABLE 7 - RATES OF SALARY INCREASES

| Years of Service | $\mathbf{2 0 1 0} \mathbf{- 2 0 1 1}$ <br> $\boldsymbol{\&}$ | $\mathbf{2 0 1 2} \mathbf{- 2 0 1 3}$ <br> \& After |
| :---: | :---: | :---: |
| 0 | 0.0650 | 0.0700 |
| 1 | 0.0650 | 0.0700 |
| 2 | 0.0650 | 0.0700 |
| 3 | 0.0650 | 0.0700 |
| 4 | 0.0650 | 0.0700 |
| 5 | 0.0650 | 0.0700 |
| 6 | 0.0650 | 0.0700 |
| 7 | 0.0650 | 0.0700 |
| 8 | 0.0650 | 0.0700 |
| 9 | 0.0650 | 0.0700 |
| 10 | 0.0550 | 0.0550 |
| 11 | 0.0550 | 0.0550 |
| 12 | 0.0550 | 0.0550 |
| 13 | 0.0550 | 0.0550 |
| 14 | 0.0550 | 0.0550 |
| 15 | 0.0400 | 0.0400 |
| 16 | 0.0400 | 0.0400 |
| 17 | 0.0400 | 0.0400 |
| 18 | 0.0400 | 0.0400 |
| 19 | 0.0400 | 0.0400 |
| $20+$ | 0.0350 | 0.0375 |

